

Panel Data Models | R programming language

Preliminaries

Script Editor

```
rm(list = ls())
directory <- "C:/Users/amalz/OneDrive/Desktop/"

# Install packages
PackageNames <- c("tidyverse", "stargazer", "magrittr", "haven")
for(i in PackageNames){
  if(!require(i, character.only = T)){
    install.packages(i, dependencies = T)
    require(i, character.only = T)
  }
}
```

Difference-in-differences model

Data: KIELMC.csv

- DID effect of building an incinerator on house prices.
- NOTE: Please read about DID models before attempting these commands.

Script Editor Deriving DID for after =0 and after =1 among treated and control units

```
KIELMC <- read.csv(paste0(directory, "KIELMC.csv"))

modell1 <- lm(formula = rprice ~ nearinc,
             data = KIELMC,
             subset = (year == 1981))
# Regression in after period (after building the incinerator)
summary(modell1)
(b1 <- coef(modell1)["nearinc"])

modell2 <- update(modell1, subset = (year == 1978))
# Regression in before period (before building the incinerator)
summary(modell2)
(b2 <- coef(modell2)["nearinc"])

b1 - b2 # Difference-in-differences effect
```

Console

```
Call:
lm(formula = rprice ~ nearinc, data = KIELMC, subset = (year ==
  1981))

Residuals:
    Min       1Q   Median       3Q      Max
-60678 -19832  -2997   21139 136754

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)  101308      3093   32.754 < 2e-16 ***
nearinc      -30688      5828   -5.266 5.14e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 31240 on 140 degrees of freedom
Multiple R-squared:  0.1653,    Adjusted R-squared:  0.1594
F-statistic: 27.73 on 1 and 140 DF, p-value: 5.139e-07

> (b1 <- coef(modell1)["nearinc"])
nearinc
-30688.27
```

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Console ctd...

```
Call:
lm(formula = rprice ~ nearinc, data = KIELMC, subset = (year ==
  1978))
```

```
Residuals:
    Min       1Q   Median       3Q      Max
-56517 -16605  -3193   8683 236307
```

```
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept)    82517      2654   31.094 < 2e-16 ***
nearinc       -18824      4745   -3.968 0.000105 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 29430 on 177 degrees of freedom
Multiple R-squared:  0.08167,    Adjusted R-squared:  0.07648
F-statistic: 15.74 on 1 and 177 DF,  p-value: 0.0001054
```

```
> (b2 <- coef(model2)["nearinc"])
nearinc
-18824.37
> b1 - b2
nearinc
-11863.9
```

Prices for houses near the incinerator were \$11,864 Lower than prices for houses far from the incinerator, after the incinerator was built.

Script Editor Deriving DID for treated =0 and treated =1 among units before and after

```
model3 <- lm(rprice ~ y81, KIELMC, nearinc == 1)
summary(model3)
(b3 <- coef(model3)["y81"])
model4 <- update(model3, subset = (nearinc == 0))
summary(model4)
(b4 <- coef(model4)["y81"])
b3 - b4
```

Running this will give the same value for DID effect (-11863.9) in the console.

Instead of manually exploring DID as shown above, the same can be done altogether at once using a comprehensive DID regression which includes treated (dummy), after(dummy), and after*treated(interaction) as variables. DID effect is the coefficient on after*treated and will be the same as calculated above.

Script Editor

```
model5 <- lm(rprice ~ nearinc + y81 + y81nrinc, KIELMC)
summary(model5)
coef(model5)["y81nrinc"]
```

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Console

```
> summary(model5)

Call:
lm(formula = rprice ~ nearinc + y81 + y81nrinc, data = KIELMC)

Residuals:
    Min       1Q   Median       3Q      Max
-60678 -17693  -3031   12483  236307

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept)    82517      2727   30.260 < 2e-16 ***
nearinc       -18824      4875   -3.861 0.000137 ***
y81           18790      4050    4.640 5.12e-06 ***
y81nrinc      -11864      7457   -1.591 0.112595
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 30240 on 317 degrees of freedom
Multiple R-squared:  0.1739,    Adjusted R-squared:  0.1661
F-statistic: 22.25 on 3 and 317 DF,  p-value: 4.224e-13

> coef(model5)["y81nrinc"]
y81nrinc
-11863.9
```

More Panel Data Models: Preliminaries

Data: JTRAIN.csv

- Example: Effect of training grants on firm scrap rate.
- Panel data where fcode is the cross sectional dimension and year is the time series dimension

Script Editor

```
rm(list = ls())
directory <- "C:/Users/amalz/OneDrive/Desktop/"
PackageNames <- c("tidyverse", "stargazer", "magrittr", "haven", "plm")
for(i in PackageNames){
  if(!require(i, character.only = T)){
    install.packages(i, dependencies = T)
    require(i, character.only = T)
  }
}
JTRAIN <- read.csv(paste0(directory, 'JTRAIN.csv'))
JTRAIN %>% filter(!is.na(lscrap)) <----- Drop missing observations for dependent variable
JTRAIN %>% select(fcode, year, lscrap, tothrs, d88, d89, grant, grant_1) <----- Keep the variables needed
JTRAIN %>% group_by(fcode) %>% summarize(n = n()) <----- Number of observations by fcode
JTRAIN %>% group_by(year) %>% summarize(n = n()) <----- Number of observations by year
JTRAIN %>%
  select(lscrap, tothrs, d88, d89, grant, grant_1) %>%
  mutate_all(function(x) {x - mean(x, na.rm = T)}) %>% # variable - overall mean
  as.data.frame %>% {----- Between variations
  stargazer(type = "text", omit.summary.stat = "mean", digits = 2)
JTRAIN %>% group_by(fcode) %>%
  select(lscrap, tothrs, d88, d89, grant, grant_1) %>%
  summarize_all(mean) %>%
  as.data.frame %>% {----- Overall variations
  select(-fcode) %>%
  stargazer(type = "text", digits = 2)
JTRAIN %>% group_by(fcode) %>%
  select(lscrap, tothrs, d88, d89, grant, grant_1) %>%
  mutate_all(function(x) {x - mean(x)}) %>% # demean
  as.data.frame %>%
  select(-fcode) %>%
  stargazer(type = "text", omit.summary.stat = "mean", digits = 2)
}
```

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Pooled OLS, between, and first differences estimator

Script Editor

```
# Pooled OLS estimator
model_ols <- plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
  data = JTRAIN,
  index = c("fcode", "year"), # c(group index, time index)
  model = "pooling")
summary(model_ols)

# Between estimator
model_be <- update(model_ols, model = "between")
summary(model_be)

# Taking first differences
diff <- function(x) {x - dplyr::lag(x)}
JTRAIN %<>%
  group_by(fcode) %>%
  mutate(dlscrap = diff(lscrap),
    dtothrs = diff(tothrs),
    dgrant = diff(grant)) %>%
  ungroup()

# First differences estimator
model_fd <- lm(dlscrap ~ dtothrs + dgrant, JTRAIN)
summary(model_fd)
```

Console

```
> summary(model_ols)
Pooling Model

Call:
plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
  data = JTRAIN, model = "pooling", index = c("fcode", "year"))

Unbalanced Panel: n = 49, T = 2-3, N = 146

Residuals:
    Min.    1st Qu.    Median     3rd Qu.     Max.
-5.081736 -0.829602 -0.071229  1.078829  3.344532

Coefficients:
              Estimate Std. Error t-value Pr(>|t|)
(Intercept)  0.6625028   0.2231918   2.9683 0.003523 **
tothrs       -0.0046484   0.0049508  -0.9389 0.349392
d88          -0.2679208   0.3256257  -0.8228 0.412028
d89          -0.5128693   0.3658318  -1.4019 0.163150
grant         0.3800988   0.3758131   1.0114 0.313568
grant_1       0.0848627   0.4491363   0.1889 0.850408
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Total Sum of Squares:    310.97
Residual Sum of Squares: 302.34
R-Squared:              0.027761
Adj. R-Squared:        -0.0069617
F-statistic: 0.799506 on 5 and 140 DF, p-value: 0.5518
```

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Console

```
> summary(model_be)
Oneway (individual) effect Between Model

Call:
plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
     data = JTRAIN, model = "between", index = c("fcode", "year"))

Unbalanced Panel: n = 49, T = 2-3, N = 146
Observations used in estimation: 49

Residuals:
    Min.   1st Qu.   Median   3rd Qu.    Max.
-3.14987 -0.87378 -0.12629  0.95121  3.03382

Coefficients: (1 dropped because of singularities)
              Estimate Std. Error t-value Pr(>|t|)
(Intercept)  1.2698730   1.7114534   0.7420   0.4620
tothrs       -0.0077291   0.0107195  -0.7210   0.4747
d88          -3.1406816   5.1105974  -0.6145   0.5420
grant         2.4888824   1.8130559   1.3728   0.1768
grant_1      -1.1938015   1.7704187  -0.6743   0.5036

Total Sum of Squares:    93.159
Residual Sum of Squares: 88.943
R-Squared:               0.045255
Adj. R-Squared:         -0.04154
F-statistic: 0.521405 on 4 and 44 DF, p-value: 0.72044
> summary(model_fd)

Call:
lm(formula = dlscrap ~ dtothrs + dgrant, data = JTRAIN)

Residuals:
    Min       1Q   Median       3Q      Max
-3.05113 -0.15989  0.05216  0.25951  2.60821

Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -0.210310   0.063422  -3.316   0.0013 **
dtothrs      -0.003297   0.002612  -1.262   0.2101
dgrant        0.045589   0.115367   0.395   0.6936
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.6034 on 93 degrees of freedom
(66 observations deleted due to missingness)
Multiple R-squared:  0.01949,    Adjusted R-squared:  -0.001597
F-statistic: 0.9242 on 2 and 93 DF,  p-value: 0.4004
```

Fixed effects within estimator

Script Editor

```
# Fixed effects within estimator
# model_fe <- update(model_ols, model = "within", effect = "individual")
model_fe <- plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
               data = JTRAIN,
               index = c("fcode", "year"), # c(group index, time index)
               model = "within", effect = "individual")
summary(model_fe)

# Summarize the individual specific effects a_i
ai <- fixef(model_fe, type = "dmean") # extract fixed effects using 'fixef'
ai %>% head(10)
summary(ai) # 'summary' shows the p-value table
data.frame(ai) %>% stargazer(type = "text") # summarize
```


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Console

```
> summary(model_fe)
Oneway (individual) effect Within Model

Call:
plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
     data = JTRAIN, effect = "individual", model = "within", index = c("fcode",
     "year"))

Unbalanced Panel: n = 49, T = 2-3, N = 146

Residuals:
    Min.    1st Qu.    Median    3rd Qu.     Max.
-2.253927 -0.142083 -0.024063  0.159263  1.412912

Coefficients:
            Estimate Std. Error t-value Pr(>|t|)
tothrs    -0.0047331  0.0029406  -1.6096  0.11092
d88        -0.0747307  0.1212112  -0.6165  0.53907
d89        -0.2182447  0.1555527  -1.4030  0.16397
grant      -0.1175244  0.1811571  -0.6487  0.51812
grant_1    -0.4097214  0.2283540  -1.7942  0.07606 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Total Sum of Squares:    31.521
Residual Sum of Squares: 24.311
R-Squared:                0.22873
Adj. R-Squared:          -0.21559
F-statistic: 5.45676 on 5 and 92 DF, p-value: 0.00019242
> # Summarize the individual specific effects a_i
> ai <- fixef(model_fe, type = "dmean") # extract fixed effects using 'fixef'
> ai %>% head(10)
      410523      410538      410563      410565      410566      410567      410577      410593
-3.27833527  0.45337572  1.29699872  0.96969656  1.14588496 -1.19438345 -0.05871249 -0.56425581
      410596      410606
      1.31942131 -1.30365914
> summary(ai) # 'summary' shows the p-value table
      Estimate Std. Error t-value Pr(>|t|)
410523 -3.2783353  0.3326591  -9.8549 4.609e-16 ***
410538  0.4533757  0.3082121   1.4710 0.1447070
410563  1.2969987  0.3100223   4.1836 6.549e-05 ***
410565  0.9696966  0.3076827   3.1516 0.0021919 **
410566  1.1458850  0.3076683   3.7244 0.0003373 ***
410567 -1.1943834  0.3076827  -3.8819 0.0001948 ***
410577 -0.0587125  0.3076418  -0.1908 0.8490661
410593 -0.5642558  0.3078266  -1.8330 0.0700321 .
410596  1.3194213  0.3086255   4.2752 4.659e-05 ***
410606 -1.3036591  0.3095618  -4.2113 5.910e-05 ***
410626 -0.6773954  0.3134209  -2.1613 0.0332689 *
410665 -3.5231088  0.3083375 -11.4261 < 2.2e-16 ***
418011  1.1072240  0.3128219   3.5395 0.0006310 ***
418021 -0.3096219  0.3095171  -1.0003 0.3197706
418035  1.1477166  0.3093131   3.7105 0.0003538 ***
418045  0.4759869  0.3696770   1.2876 0.2011234
418051 -1.0252676  0.3100117  -3.3072 0.0013454 **
418054 -0.1049205  0.3095171  -0.3390 0.7353962
418065 -0.1138331  0.3091246  -0.3682 0.7135377
418076 -0.7083632  0.3300305  -2.1464 0.0344758 *
418083  0.2771049  0.3741704   0.7406 0.4608312
418091  0.0799539  0.3101662   0.2578 0.7971542
418097  0.0068739  0.3091242   0.0222 0.9823073
418107 -0.7154665  0.3175040  -2.2534 0.0266090 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> data.frame(ai) %>% stargazer(type = "text") # summarize

=====
Statistic N  Mean  St. Dev.  Min    Max
-----
ai          49  0.002  1.404    -3.523  2.722
=====
```

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Dummy variables regression

Script Editor

```
# Dummy variables regression with fixed effects
# model_dv <- update(model_ols, ~ . + factor(fcode))
model_dv <- plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1 + factor(fcode),
  data = JTRAIN,
  index = c("fcode", "year"), # c(group index, time index)
  model = "pooling")
summary(model_dv)
```

- `factor(fcode)` creates one dummy variable for each `fcode`. Results will be similar to fixed effects estimator shown above.

Random effects estimator

Script Editor

```
# Random effects estimator
# model_re <- update(model_ols, model = "random", random.method = "walhus")
model_re <- plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
  data = JTRAIN,
  index = c("fcode", "year"), # c(group index, time index)
  model = "random", random.method = "walhus")
summary(model_re)
# Calculate the random effects parameter theta
(sigma2_e <- model_re$ercomp$sigma2["idios"])
(sigma2_u <- model_re$ercomp$sigma2["id"])
(theta <- 1 - sqrt(sigma2_e / (sigma2_e + 3*sigma2_u)))
```

Console

Oneway (individual) effect Random Effect Model
(Wallace-Hussain's transformation)

Call:
plm(formula = lscrap ~ tothrs + d88 + d89 + grant + grant_1,
data = JTRAIN, model = "random", random.method = "walhus",
index = c("fcode", "year"))

Unbalanced Panel: n = 49, T = 2-3, N = 146

Effects:

	var	std.dev	share
idiosyncratic	0.2553	0.5053	0.118
individual	1.9172	1.3846	0.882

theta:

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
theta	0.7501	0.7938	0.7938	0.7932	0.7938	0.7938

Residuals:

	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
Residuals	-2.51427	-0.19917	-0.00172	-0.00019	0.27108	1.59999

Coefficients:

	Estimate	Std. Error	z-value	Pr(> z)
(Intercept)	0.6638756	0.2166307	3.0646	0.00218 **
tothrs	-0.0047381	0.0028041	-1.6897	0.09108 .
d88	-0.0915398	0.1194667	-0.7662	0.44354
d89	-0.2483872	0.1517170	-1.6372	0.10159
grant	-0.0741720	0.1751030	-0.4236	0.67186
grant_1	-0.3546065	0.2203972	-1.6089	0.10763

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Total Sum of Squares: 43.404

Residual Sum of Squares: 36.353

R-Squared: 0.16246

Adj. R-Squared: 0.13255

Chisq: 27.1435 on 5 DF, p-value: 5.3487e-05

```
> (sigma2_e <- model_re$ercomp$sigma2["idios"])
```

```
  idios
```

```
0.2553429
```

```
> (sigma2_u <- model_re$ercomp$sigma2["id"])
```

```
  id
```

```
1.917162
```

```
> (theta <- 1 - sqrt(sigma2_e / (sigma2_e + 3*sigma2_u)))
```

```
  idios
```

```
0.7938235
```

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Hausman test for fixed versus random effects

- The Hausman test is used to decide whether to use fixed effects or random effects.
- H_0 : FE coefficients are not significantly different from the RE coefficients
- H_a : FE coefficients are significantly different from the RE coefficients
- If the Hausman test statistic is insignificant, use RE estimator because it is efficient
- If the Hausman test statistic is significant, use FE estimator because it is consistent

Script Editor

```
# Fixed effects estimator
summary(model_fe)
# Random effects estimator
summary(model_re)
# Hausman test for fixed versus random effects
phtest(model_fe, model_re)
```

Summary of both models have already been showcased before. Hence, only Hausman test displayed here.

Console

```
> # Hausman test for fixed versus random effects
> phtest(model_fe, model_re)

Hausman Test

data:  lscrap ~ tothrs + d88 + d89 + grant + grant_1
chisq = 1.225, df = 5, p-value = 0.9425
alternative hypothesis: one model is inconsistent
```